

# Active vorticity control in a shear flow using a flapping foil

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It is shown experimentally that free shear flows can be substantially altered through direct control of the large coherent vortices present in the flow.

First, flow-visualization experiments are conducted in Kalliroscope fluid at Reynolds number 550. A foil is placed in the wake of a D-section cylinder, sufficiently far behind the cylinder so that it does not interfere with the vortex formation process. The foil performs a heaving and pitching oscillation at a frequency close to the Strouhal frequency of the cylinder, while cylinder and foil also move forward at constant speed. By varying the phase of the foil oscillation, three basic interaction modes are identified. (i) Formation of a street of pairs of counter-rotating vortices, each pair consisting of one vortex from the initial street of the cylinder and one vortex shed by the foil. The width of the wake is then substantially increased. (ii) Formation of a street of vortices with reduced or even reverse circulation compared to that of oncoming cylinder vortices, through repositioning of cylinder vortices by the foil and interaction with vorticity of the opposite sign shed from the trailing edge of the foil. (iii) Formation of a street of vortices with circulation increased through merging of cylinder vortices with vortices of the same sign shed by the foil. In modes (ii) and (iii) considerable repositioning of the cylinder vortices takes place immediately behind the foil, resulting in a regular or reverse Kármán street. The formation of these three interaction patterns is achieved only for specific parametric values; for different values of the parameters no dominant stable pattern emerges.

Subsequently, the experiments are repeated in a different facility at larger scale, resulting in Reynolds number 20000, in order to obtain force and torque measurements. The purpose of the second set of experiments is to assess the impact of flow control on the efficiency of the oscillating foil, and hence investigate the possibility of energy extraction. It is found that the efficiency of the foil depends strongly on the phase difference between the oscillation of the foil and the arrival of cylinder vortices. Peaks in foil efficiency are associated with the formation of a street of weakened vortices and energy extraction by the foil from the vortices of the vortex street.

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## 1. Introduction

Flow control is currently attracting increased attention in connection with a variety of applications. In flow control applications one may want to destabilize the flow, in order to achieve better mixing, or to stabilize the flow in order to eliminate undesirable unsteady loads. Several studies have appeared on the subject, and one can classify the

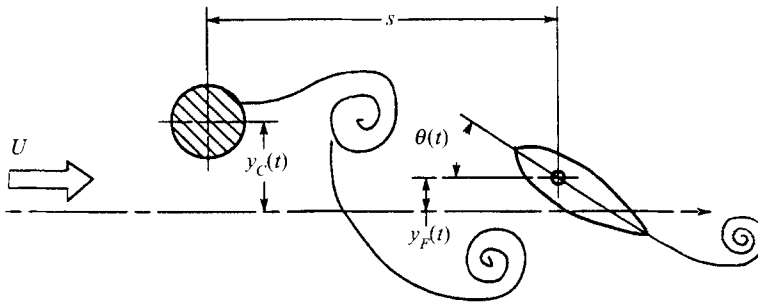


FIGURE 1. Sketch of the concept tested. An oscillating symmetric foil is placed in the wake of a cylinder oscillating transversely. Cylinder and foil also move forward at constant speed.

techniques used into two major categories: passive control, in which flow control is achieved by altering the geometry of the flow; and active control, in which a time-dependent forcing is applied to the flow, by means, for instance, of a loudspeaker.

Passive control can suppress unsteadiness in a flow (as demonstrated by Chen & Templin 1974; Zdravkovich 1981; Strykowski & Sreenivasan 1990). In practical applications, however, no matter how careful the design is, flow separation and unsteadiness behind moving bodies are often unavoidable because of manoeuvring motions, or encountering ambient turbulence. The possibility of actively controlling a flow has thus been studied by several researchers.

Active control can be divided into open loop schemes, in which the forcing is a prescribed function of time, and closed-loop schemes, in which the forcing is a function of some real-time measurement of the response of the flow. Open-loop schemes rely on an accurate knowledge of the basic fluid mechanics of the problem in order to prescribe the appropriate forcing function for the controller (see Tokumaru & Dimotakis 1991 as a paradigm of effective use of this method). In closed-loop schemes, on the other hand, a sensor device is placed in the flow field, and its signal, after going through a controller, is fed to the actuator device (see e.g. Ffowcs Williams & Zhao 1989). Closed-loop schemes thus do not necessarily require the detailed knowledge of fluid mechanics that open-loop schemes do, but, in addition to the issue of closed-loop stability, the very important question of observability of the flow remains open. In fact, Roussopoulos (1993) has recently presented convincing evidence that, when a single sensor is used, the flow is not observable, in the sense that unsteady patterns are present without being detected by the sensor.

In this paper we investigate an active flow control concept, which relies on directly controlling the coherent vortices present in high Reynolds number flows. The goal here is to reposition these vortices and change their strength in a way that is considered desirable. Herein open-loop studies are reported only. In order to demonstrate the concept and to study the basic fluid mechanics involved, we conducted a generic experiment which aimed at altering the vortex street produced by a bluff object through the use of an oscillating foil, placed in the wake of the object. Previously, stationary foils have been used as vortex splitting devices in boundary-layer control (see among others, Corke, Guezennec & Nagib 1979; Hefner, Weinstein & Bushnell 1979; Dowling 1985). An oscillating foil was used by Koochesfahani & Dimotakis (1988) to cancel the effect of an externally imposed harmonic perturbation in a mixing layer.

In the following sections we provide experimental evidence that, by appropriately adjusting the phase of the oscillating foil, it is feasible to alter the strength and position of the vortices of the Kármán vortex street downstream of the foil, thus creating new

vortical patterns in the wake. The investigation consists of two parts: (a) flow-visualization experiments, at Reynolds number 550, in which the interaction modes between the oscillating foil and the vortex street are identified, and (b) force-measuring experiments, in which the effect of the modes identified in part (a) on the forces acting on the foil and the resulting efficiency are investigated.

Apart from demonstrating the feasibility of flow control, the results of the experiments reported in this paper can be used to interpret observations in the hydrodynamics of fish swimming, since the oscillating foil can be loosely thought of as simulating the effect of the tail of the fish, which controls the vorticity generated by the main body of the fish (Rosen 1959), with the intent of recovering some of the energy lost in forming these vortices.

## 2. Description of experiments

In order to demonstrate that vortices can be controlled directly, in the sense of altering their position and strength; and also that energy can be extracted from large-scale patterns, we devised the following experimental scheme, shown in figure 1. A cylinder with a D-shaped cross-section, with the flat part of the D facing downstream, is towed at constant speed in order to generate a Kármán vortex street. The cylinder is oscillated at a frequency close to its Strouhal number so that strong, well-correlated vortices are formed in its wake. A D-section cylinder was selected, instead of a circular cylinder, in order to avoid the large-amplitude swinging motion of the base region, observed in circular cylinders (Ongoren & Rockwell 1988). It was also found that within a small range around the frequency tested, the phase of the formed vortices was constant, hence providing good vortex-formation phase control.

A symmetric foil is placed in the wake of the cylinder, at a sufficiently large distance downstream of the cylinder to avoid interference with the formation region of the cylinder. The foil oscillates in a combined transverse motion (heave) and rotational motion (pitch). The average transverse position of the foil and the cylinder are on a line parallel to the direction of forward motion. For experimental simplicity, the same transverse motion was imposed on the cylinder and the foil, while their relative distance along the direction of motion (longitudinally) was kept constant in each experiment, but was allowed to vary between experiments. The longitudinal distance between cylinder and foil determines the specific transverse position and pitch angle of the oscillating foil when it encounters oncoming cylinder vortices at its leading edge, and is thus the main control parameter in the experiment.

Two different tanks were used to study vorticity control, a small tank (2.44 m in length) used for visualization, and a larger tank (30 m in length) used to measure forces on the foil. The apparatus used in both cases was geometrically similar, except for the span to diameter ratio.

The cylinder (of diameter  $d$  and span  $l$ ) is forced to oscillate with displacement  $y_C(t)$ :

$$y_C(t) = A_C \sin(2\pi f_C t), \quad (1)$$

where  $A_C$  is the oscillation amplitude, and  $f_C$  is the oscillation frequency. The foil, of chord length  $c$ , and span equal to the cylinder span, is placed at a distance  $s$  behind the cylinder and subjected to a combined transverse translation (heave) and rotation (pitch). The heave displacement,  $y_F(t)$ , is given as:

$$y_F(t) = A_F \sin(2\pi f_F t + \psi), \quad (2)$$

where  $A_F$  denotes the amplitude,  $f_F$  the frequency and  $\psi$  the phase angle between the

motion of the foil and that of the cylinder. The pitching motion of the foil,  $\theta(t)$ , has the same frequency  $f_F$  as the heave motion, its pivot point is at a distance  $p$  from the leading edge, and it is given as:

$$\theta(t) = \theta_F \sin(2\pi f_F t + \psi + \phi), \quad (3)$$

where  $\phi$  denotes the phase angle between the pitching and heaving motions of the foil. The system operates in a uniform flow of free-stream velocity  $U$ . The Reynolds number was  $\approx 550$  for the flow-visualization experiments and  $\approx 20000$  for the force measurement experiments.

One cylinder and two foil models were fabricated, providing foil chord to cylinder diameter geometric ratios  $c/d$  of 1 and 2, respectively. Most tests were performed with the larger foil ( $c/d = 2$ ), since preliminary visualization experiments showed that the smaller foil ( $c/d = 1$ ) produced very weak vortex interactions.

Three values of cylinder oscillation amplitude ratio were selected to ensure strong lock-in vortex shedding; these were  $A_C/d = 0.500, 0.667, \text{ and } 0.833$ . Since the same heaving mechanism was used to oscillate both the cylinder and the foil,  $A_C = A_F, f_C = f_F$ , and  $\psi = 0$ . Because  $\psi$  was fixed, the separation length ratio  $s/d$  was made highly variable (21 discrete values between 1.5 and 8.0) so as to control the arrival time of cylinder vortices at the foil leading edge, to correspond to different phases of the foil motion. These simplifications limited somewhat our ability for vorticity control, for example by not being able to control the strength of the foil vortices independently. However, the phasing between the arrival of the vortices and the motion of the foil, which is the principal control parameter, could be varied in an almost continuous manner.

Fixed values were chosen for the model aspect ratios and foil pivot point. The cylinder aspect ratio,  $l/d$ , was 5.33 for the flow visualization experiments and 12.00 for the force measurement experiments, while the larger foil aspect ratio,  $l/c$ , was 2.67 for the flow-visualization experiments and 6.00 for the force-measurement experiments. The ratio of the distance of the foil pivot point from the leading edge to the chord length,  $p/c$ , was chosen to be 0.33 in all cases.

The design of the foil pitching oscillator used in the flow-visualization experiments allowed the following discrete values of pitch amplitude  $\theta$ :  $0^\circ, 7^\circ, 15^\circ, 30^\circ, 45^\circ$  and  $60^\circ$ . Of these allowable values, most runs were conducted with  $\theta$  at  $15^\circ, 30^\circ$  or  $45^\circ$ .

Based on earlier experiments on a flapping foil (Triantafyllou *et al.* 1991, 1993), which showed that optimal efficiency is achieved when the phase angle  $\phi$  between the foil pitching and heaving motions is between  $70^\circ$  and  $100^\circ$ , a value of  $90^\circ$  was used for this phase angle throughout. In order to ensure strong lock-in vortex generation, the experiments were conducted at cylinder Strouhal numbers very close to  $f_C d/U = 0.20$ .

As a result of the simplifications noted above, the experiments were conducted with different combinations of the following parameters: motion amplitude to diameter ratio  $A_C/d$ , cylinder Strouhal number  $f_C d/U$ , pitch amplitude  $\theta$ , and separation length  $s/d$ . The principal control parameter in the problem was found to be the separation length ratio  $s/d$ .

### 3. Flow-visualization experiments

In order to conduct flow-visualization experiments, a small tank was used together with a commercially available Kalliroscope fluid. This fluid is a very dilute colloidal suspension of organically derived guanine flakes in water. The guanine flakes have a typical dimension of  $6 \times 30 \times 0.07 \mu\text{m}^3$ ; thus they are very small and have a highly

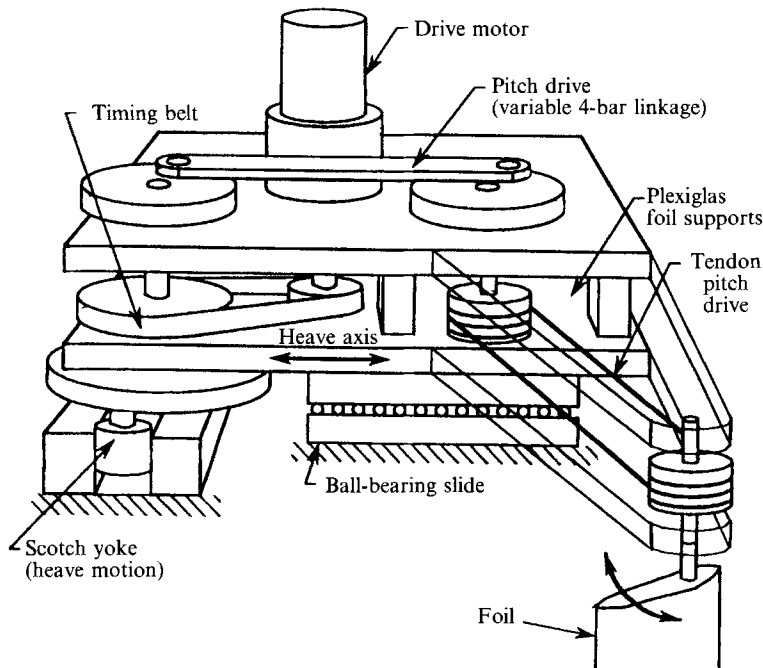


FIGURE 2. The oscillating mechanism used in the Kalliroscope tank to impart the same transverse (heave) motion on the cylinder and the foil, while allowing the foil to pitch at variable amplitude and phase relative to the heave motion. Pitching is produced through an oscillating 4-bar linkage. Heaving is driven by a rotating scotch yoke. Both motions are powered by a single variable-speed motor.

anisotropic shape. The specific gravity of guanine is about 1.62, and the observed sedimentation velocity of Kalliroscope flakes in water is about 0.1 cm/h (Matisse & Gorman 1984). We added a blue aqueous dye to the water to aid in the visualization.

Gorman & Swinney (1982) used Kalliroscope fluid to visualize the onset of weak turbulence in the circular Couette system. They found that the Kalliroscope platelets align with the flow, and the intensity of the scattered light measured with their Kalliroscope fluid apparatus had the same features as earlier velocity measurements using a laser Doppler velocimeter, while the influence of the suspension on the properties of pure water was less than 0.1% (Matisse & Gorman 1984). Savaş (1985) performed a stochastic analysis of the motion of thin, ellipsoidal particles in a viscous fluid, with a view to predicting the observed light field in flow-visualization experiments. He concluded that in the presence of a shear flow, the flakes align themselves to be parallel to the stream surfaces, which are thus revealed in the visualization. He also showed that this technique of using small suspended particles is unsuitable for visualizing flows involving small-amplitude perturbations to backgrounds with high shear, e.g. Tollmien–Schlichting waves in a boundary layer. The Kalliroscope fluid was well suited to the experiments reported herein, i.e. for visualizing vortex flows, which are large-scale, high shear perturbations over uniform background flows.

In order to utilize the Kalliroscope fluid, a smaller visualization tank was constructed. The *K*-tank (as we shall call it for brevity) consisted of a rectangular Plexiglas structure of dimensions  $2.44 \times 0.60 \times 0.15$  m<sup>3</sup>. A small, belt-driven carriage was constructed to ride over the *K*-tank, supported rigidly by linear ball bearings on one side and a single cam follower on the other side. A d.c. motor was employed to provide the motive force to the towing belt, and allowed constant carriage velocities of

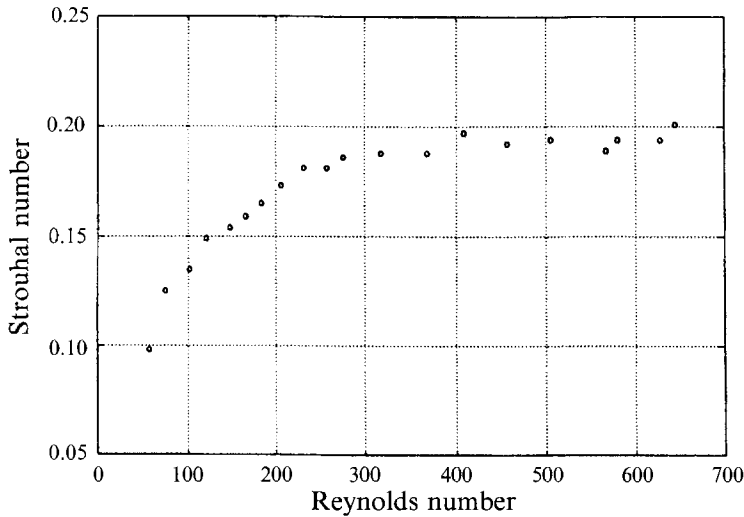


FIGURE 3. Measured Strouhal number for a stationary D-section cylinder moving forward at constant speed, as function of Reynolds number.

up to  $0.15 \text{ m s}^{-1}$ . An oscillation mechanism, similar to the experimental apparatus of Freymuth (1990), was designed and implemented. Figure 2 is a schematic illustration of this mechanism, which allowed for both translation (heaving) and rotation (pitching) motions to be provided by a single d.c. motor. Independently adjustable settings provided for a heave amplitude of up to 3.81 cm, a pitch angle amplitude of up to  $60^\circ$ , and an oscillation frequency of up to 0.35 Hz. A number of values for the phase angle  $\phi$  could be set; we used only the setting of  $90^\circ$ . The oscillation mechanism was installed on the towing carriage, and the cylinder and foil models were suspended vertically into the fluid, via a mounting assembly that provided for close control of the separation length between the models. The *K*-tank was illuminated by diffuse lighting from overhead fluorescent sources. A high-resolution black-and-white video camera was mounted on a tripod bolted to the carriage, enabling video recordings of the wake patterns to be obtained from a frame of reference moving with the carriage. Still photographs of the wake were obtained off a TV monitor while playing back the video recordings.

### 3.1. Experimental results

Little information exists in the literature on the behaviour of vortex formation behind a D-section cylinder, so we first conducted a number of stationary (non-oscillating) tests with the D-section cylinder alone. The cylinder has diameter 1.91 cm and span 10.15 cm. The model was towed at different speeds through the Kalliroscope fluid and the vortices shed over a specific distance were counted, in order to determine the Strouhal number. Figure 3 shows that the form and values of the curve depicting the Strouhal number versus the Reynolds number for the D-section cylinder is similar to the corresponding curve for a circular cylinder. Hoerner (1965, p. 3.17) lists an average drag coefficient of 1.16 for a D-section cylinder, which is also very close to the value of 1.17 listed for a circular cylinder.

Tests with a D-section and hydrofoil tandem arrangement proved that the D-section indeed performed its intended role of generating strong vortices without disrupting the flow upstream of the foil, i.e. the street vortices were formed behind the cylinder without noticeable change compared to the case of towing the cylinder alone. When the

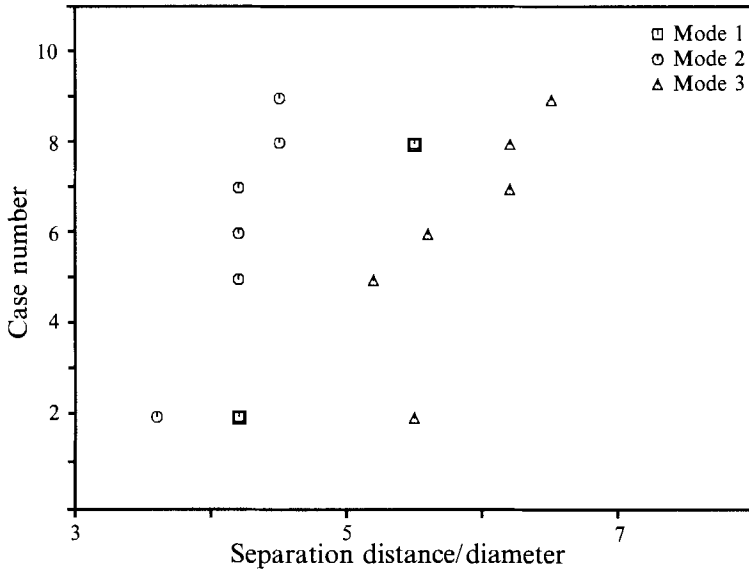


FIGURE 4. Modes 1, 2 and 3 as function of the relative spacing between cylinder and foil. The numbers at the vertical axis denote the corresponding condition described in table 1.

Number	Heave ( $A_c/d$ )	Pitch ( $\theta$ )	Strouhal number ( $S_F$ )	Angle of attack ( $\alpha$ )
1	0.500	15°	0.246	+16.86
2	0.500	30°	0.354	+01.86
3	0.500	45°	0.483	-13.14
4	0.667	15°	0.302	+24.65
5	0.667	30°	0.395	+09.65
6	0.667	45°	0.509	-05.35
7	0.833	15°	0.358	+31.01
8	0.833	30°	0.441	+16.01
9	0.833	45°	0.550	+01.01

TABLE 1. Heave and pitch amplitude combinations tested.

cylinder was forced to oscillate transversely, the phase of the vortex formation (relative to the cylinder oscillation) was found to depend very weakly on the oscillation frequency, within a small range bracketing the Strouhal number of 0.20. Hence, small variations in frequency were not of importance and all runs were conducted at Strouhal numbers close to 0.20. The Reynolds number  $Rn$ , based on the cylinder diameter, was about 550 for all experiments, which is well beyond the  $Rn$  region over which there is rapid Strouhal number variation, as shown in figure 3.

The foil used has a NACA 0012 shape with zero camber, chord length 3.81 cm and span equal to the cylinder span. Tests were conducted over a grid of parameters consisting of three heave-amplitude settings, three pitch-amplitude settings, and twenty separation lengths. For each combination of heave and pitch amplitude, we calculated the nominal foil Strouhal number  $S_F$ :

$$S_F = \frac{f_F A}{U}, \quad (4)$$

where  $A$  denotes the total excursion of the trailing edge of the foil. We employ the term

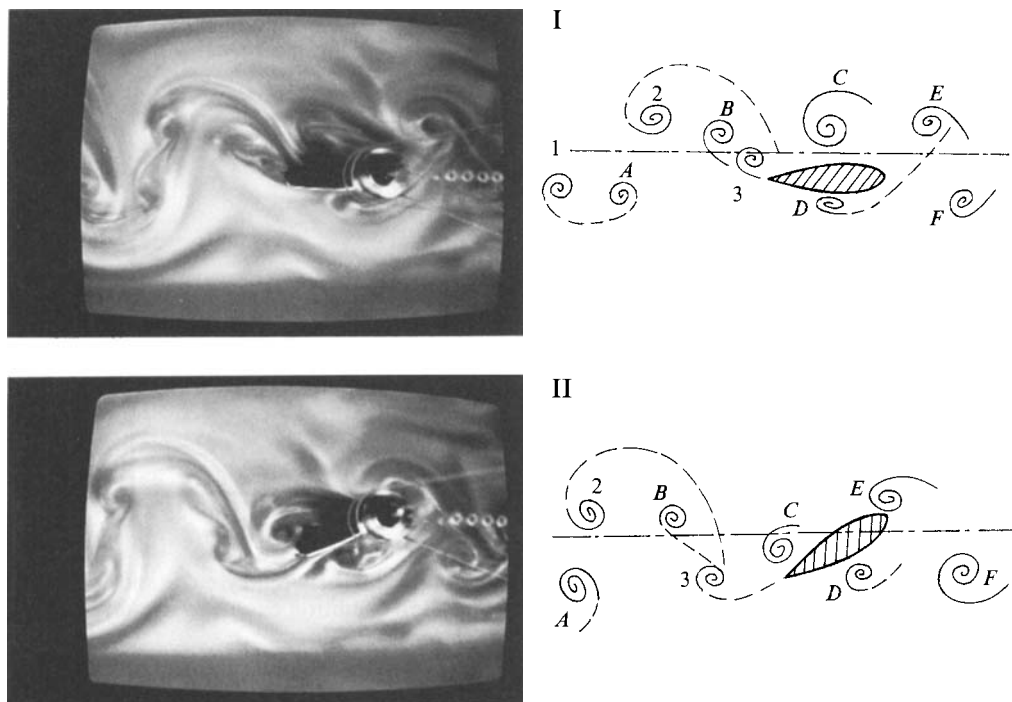


FIGURE 5. Wake interaction mode 1. Four views are presented for each mode, at time intervals equal to one quarter the period of foil oscillation. Views I and II are shown here. The cylinder and foil are moving from left to right. The cylinder is at the right-hand edge of the photograph, the foil is visible behind, attached to the carriage through a structure made of transparent plastic. The sketch beside the photograph depicts the principal features. Each cylinder vortex joins up with a newly formed foil vortex of the opposite sign to form a pair, thus a street of vortex pairs is formed, resulting in an expanding wake. In all drawings, the cylinder's Kármán vortices are labelled with letters (*A*, *B*, *C*, etc.), while the foil vortices are labelled with numerals (1, 2, 3, etc.). At instant I, the foil is at the bottom of its heave stroke. Cylinder vortex *C* has been moved down from its upstream position owing to foil suction, and foil vortex 3 is in the process of formation. The foil has just encountered cylinder vortex *D* near the leading edge. Instant II is taken when the foil is at the centreline, moving upwards. Foil vortex 3 has been shed into the wake, and cylinder vortex *C* is being rolled off the trailing edge. Cylinder vortex *D* is now trapped by the foil suction and is moving upwards from its original position.

*nominal Strouhal number* since the actual flow velocity at the foil was not measured; instead, the free-stream velocity  $U$  has been used in the calculations. Table 1 lists the heave- and pitch-amplitude combinations tested; each entry of the table was repeated for 20 separation length settings.

It was found that the oscillating foil altered substantially the position and strength of the incoming cylinder vortices. We note again that the effect of the foil on the vortices was felt only near and downstream of the foil, while the near wake of the cylinder was not changed noticeably. We identified the following three distinct stable modes:

1. Expanding wake, when oncoming cylinder vortices pair up with vortices shed by the foil to form 'mushroom'-like structures, drifting away transversely to the flow.
2. Destructive interaction, when oncoming cylinder vortices are repositioned by the foil and they interact with vorticity of the opposite sign shed by the trailing edge of the foil, to form ultimately weakened vortices, or even vortices of the opposite circulation.
3. Constructive interaction, when oncoming cylinder vortices merge with vortices of



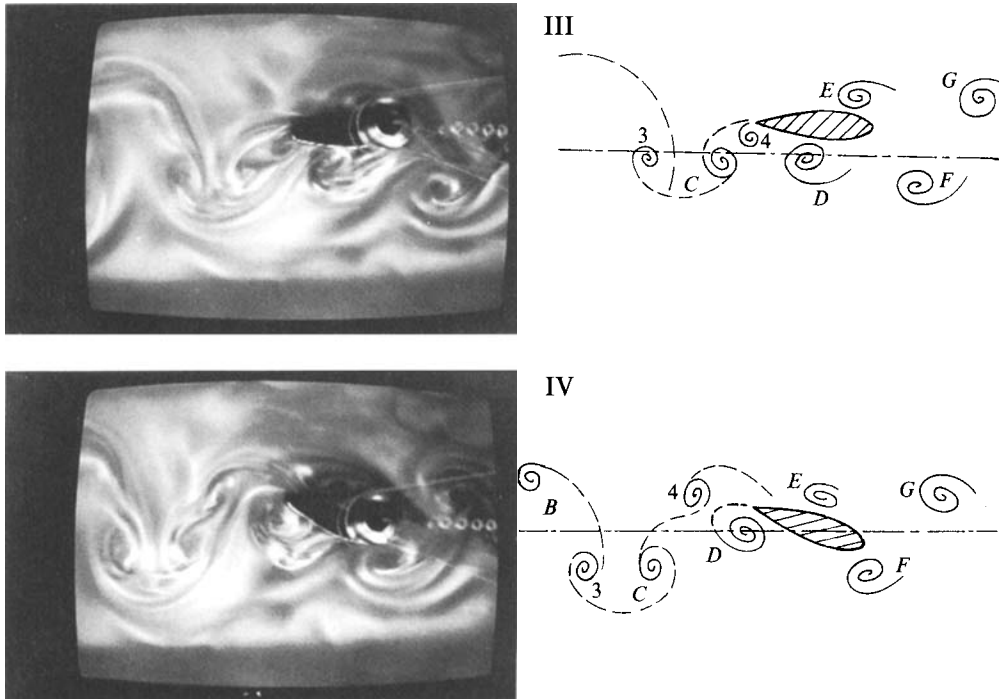


FIGURE 6. Wake interaction mode 1, views III and IV. View III is taken when the foil is at the top of its heave stroke. Cylinder vortex  $C$  has moved downstream from the trailing edge of the foil, and is joined with foil vortex 3 of the opposite rotational sign. Foil vortex 4 forms at the trailing edge, while cylinder vortex  $D$  has been repositioned. In view IV the foil is at the centreline, moving down. Foil vortex 4 has been shed from the trailing edge, and cylinder vortex  $D$  forms a pair with vortex 4. Pair 3- $C$  is convecting slowly downstream and away from the wake centreline. Just upstream of the foil, vortex  $E$  is trapped by the foil suction and is moving downwards; at an instant  $\frac{1}{4}T$  later it will assume the position of vortex  $C$  of view I of figure 5 and the cycle will repeat.

the same sign shed by the foil to form much stronger vortices compared to their original strength.

Figure 4 shows the various combinations of the principal parameters at which the above modes were found. The horizontal axis of the figure refers to the spacing, i.e. the separation length between the cylinder and the foil, measured between the rear face of the D-section cylinder and the pivot point on the foil, divided by the cylinder diameter. The vertical axis provides the case number tested, with reference to the conditions listed in table 1. Figure 4 shows that the spacing  $s/d$  is the most important parameter, and for certain combinations of heave and pitch, it was possible to achieve more than one mode by varying  $s/d$  suitably.

We discuss next the principal features of each of the three modes since they constitute major patterns for flow control.

### 3.1.1. Mode 1: Expanding wake

In this mode each oncoming cylinder vortex joins up with a newly formed foil vortex of the opposite sign to form a pair, slowly drifting away from the centreline of the wake, owing to the mutual velocity induction. Thus a street of vortex pairs is formed, resulting in an expanding wake.

The formation of vortex pairs is illustrated in figures 5 and 6. The figures show a sequence of photographs of the wake taken at instants of time approximately  $\frac{1}{4}T$  apart,

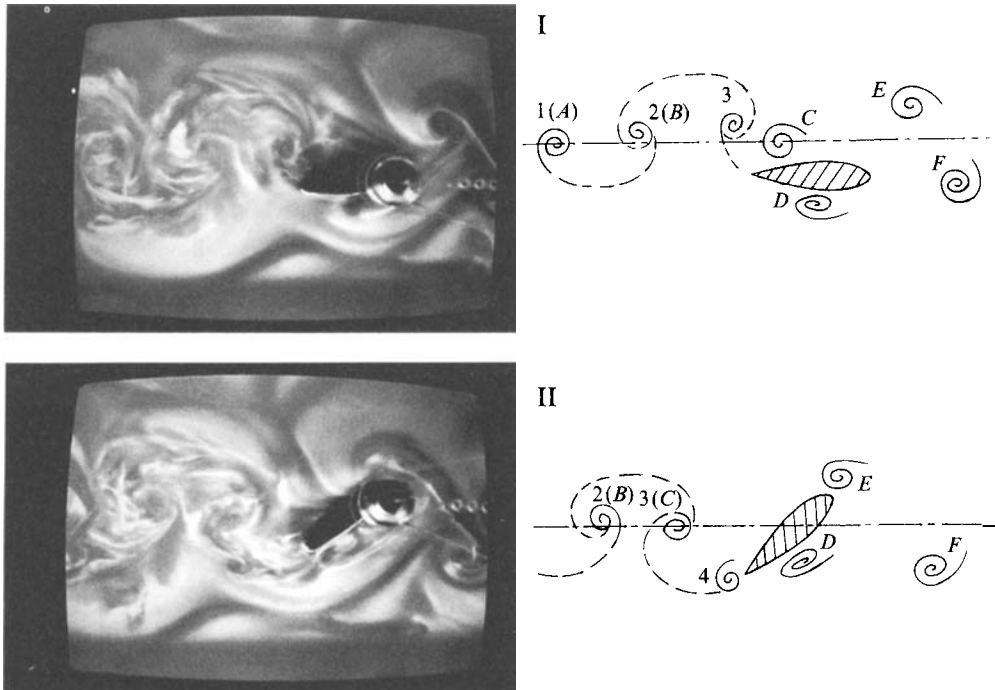


FIGURE 7. Wake interaction mode 2, views I and II. Cylinder vortices are repositioned by the foil and interact with vorticity of opposite rotational sign shed by the trailing edge of the foil. In I the foil is at the bottom of its heave stroke, and a strong vortex is seen forming off the trailing edge (3). Cylinder vortex *C* is slightly below and upstream of vortex 3. Cylinder vortex *D* is below the leading edge of the foil. View II is taken when the foil is at the centreline and moving up. Vorticity shed by the foil (3) has interacted destructively with cylinder vortex *C*. Foil vortex 4 is being formed at the trailing edge, while cylinder vortex *D* is being repositioned upwards. The foil is about to encounter cylinder vortex *E* near its leading edge.

where  $T = 1/f_F$  is the time period of the oscillation. The photographs focus on the region of the wake surrounding the oscillating foil, and show the vortex patterns both upstream and downstream of the foil. The direction of towing is from left to right, giving an equivalent free-stream velocity from right to left. Hand-drawn figures of the vortex positions accompany the photographs, to clarify the evolution of the process. In all drawings, the cylinder's Kármán vortices (coming from upstream) are labelled with letters (*A*, *B*, *C*, etc.), while the foil vortices are labelled with numerals (1, 2, 3, etc.).

Figure 5 illustrates the instants I and II of the cycle. At instant I, the foil is at the bottom of its heave stroke. In the first view, cylinder vortex *C* has moved down from its upstream position (owing to foil suction), while foil vortex 3 is in the process of formation. In addition, the foil has just encountered cylinder vortex *D* near the leading edge. Instant II is taken at time  $\frac{1}{4}T$  later, when the foil is at the centreline, moving upwards. Foil vortex 3 has been shed into the wake, and cylinder vortex *C* is being rolled off the trailing edge as well. Cylinder vortex *D* is now trapped by the foil suction and is moving upwards from its original position.

Figure 6 illustrates instants III and IV of the cycle. View III is taken at time  $\frac{1}{4}T$  later and the foil is now at the top of its heave stroke. Cylinder vortex *C* has moved downstream from the trailing edge of the foil, and is joined with foil vortex 3 of the opposite rotational sign. Foil vortex 4 is in the process of formation from the trailing

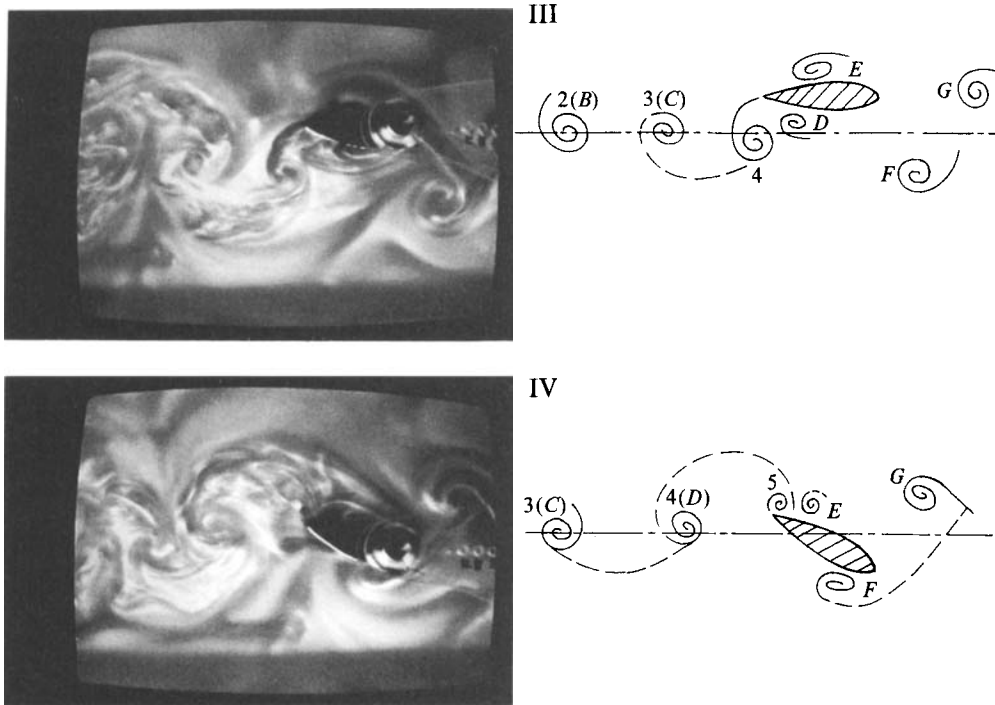


FIGURE 8. Wake interaction mode 2, views III and IV. View III, shows the foil at the top of its heave motion. Foil vortex 4 is seen behind the trailing edge; cylinder vortex  $D$  lies just above and in front of vortex 4. Cylinder vortex  $E$  is above the leading edge of the foil. View IV shows the foil at the wake centreline, on its way down. Vorticity shed by the foil (4) has weakened as a result of interaction with cylinder vortex  $D$  and is well into the wake. Foil vortex 5 is in the process of formation, while cylinder vortex  $E$  is being repositioned by the foil suction. The composite vortices 3(C) and 4(B) are nearly aligned within the wake.

edge, while cylinder vortex  $D$  has been repositioned by the suction of the foil. View IV shows the final instant of the sequence. The foil is at the centreline, moving down. Foil vortex 4 has been shed from the trailing edge, and cylinder vortex  $D$  is swept to form a pair with vortex 4. Downstream of the foil, the vortex pair 3-C convects slowly away from the wake centreline. Just upstream of the foil, vortex  $E$  is trapped by the foil suction and moves downwards; at an instant  $\frac{1}{4}T$  later it will assume the position of vortex  $C$  of view I of figure 5 and the cycle will repeat.

### 3.1.2. Mode 2: Destructive interaction

Mode 2 is characterized by a destructive interaction, where cylinder vortices are repositioned by the foil and they interact with vorticity shed by the foil, which is of opposite rotational sign. The resulting vortices have smaller circulation than, or even opposite circulation to, the oncoming cylinder vortices, and form a vortex street with small lateral spacing, and hence small induced in-line wake velocity. Depending on the strength of the foil vortices, the configuration downstream of the foil was of the thrust type (reverse Kármán street) or of the drag type (Kármán street).

A destructive interaction is illustrated by the sequence of photographs and drawings in figures 7 and 8. As before, each figure contains two photographs taken at instants  $\frac{1}{4}T$  apart in time, for a total sequence of four views. The free-stream velocity is from right to left.

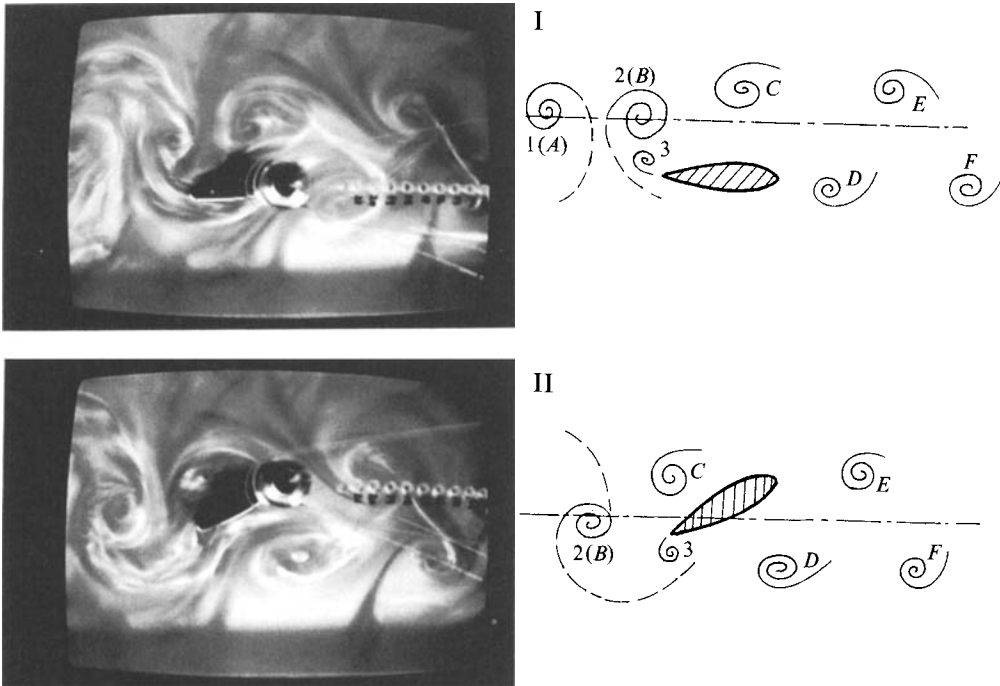


FIGURE 9. Wake interaction mode 3, views I and II. The third mode is characterized by vortex merging. In view I the foil is at the bottom of the heave stroke. Foil vortex 2 has merged with cylinder vortex ( $B$ ). Cylinder vortex  $C$  is located above the foil. View II shows that the merged vortex  $2(B)$  has moved into the wake. Vortex 3 is forming at the trailing edge of the foil, which is now at the centreline and moving up. Cylinder vortex  $C$  is being swept back over the foil, and will eventually merge with vortex 3. Cylinder vortex  $D$  is as yet too far away to be affected by the suction of the foil.

Starting with view I of figure 7, where the foil is at the bottom of its heave stroke, a strong vortex is seen forming off and still connected to the trailing edge, labelled as foil vortex 3. Cylinder vortex  $C$  is seen slightly below and just upstream of vortex 3, and is interacting with it and the feeding layer. Cylinder vortex  $D$  is below the leading edge of the foil. View II shows the situation at an instant of time  $\frac{1}{4}T$  later; the foil is now at the centreline and moving up. The cylinder vortex  $C$  has interacted destructively with vorticity shed by the foil (3) and is now well into the wake. Foil vortex 4 forms now at the trailing edge, while cylinder vortex  $D$  is trapped below the trailing edge and is repositioned upwards. Also, the foil is about to encounter cylinder vortex  $E$  near its leading edge.

The sequence is continued in figure 8, which contains views III and IV. View III, shows the foil at the top of its heave motion. Foil vortex 4 is clearly seen forming behind the trailing edge; cylinder vortex  $D$  lies just above and upstream of vortex 4. Cylinder vortex  $E$  is now above the leading edge of the foil and is partly obscured by the shadow of the foil in the photograph. View IV shows the foil at the wake centreline, on its way down. Vortex  $D$  (which has interacted with vorticity shed by the foil, marked as vortex 4) is well into the wake. Foil vortex 5 is in the process of formation, while cylinder vortex  $E$  is being repositioned by the foil suction. A street of vortices is observed downstream of the foil, which are marked by the number and letter of the interacting foil and cylinder vortices, respectively. Hence the vortices marked  $3(C)$  and  $4(B)$  are the final result of interaction between oncoming cylinder vortices and vorticity

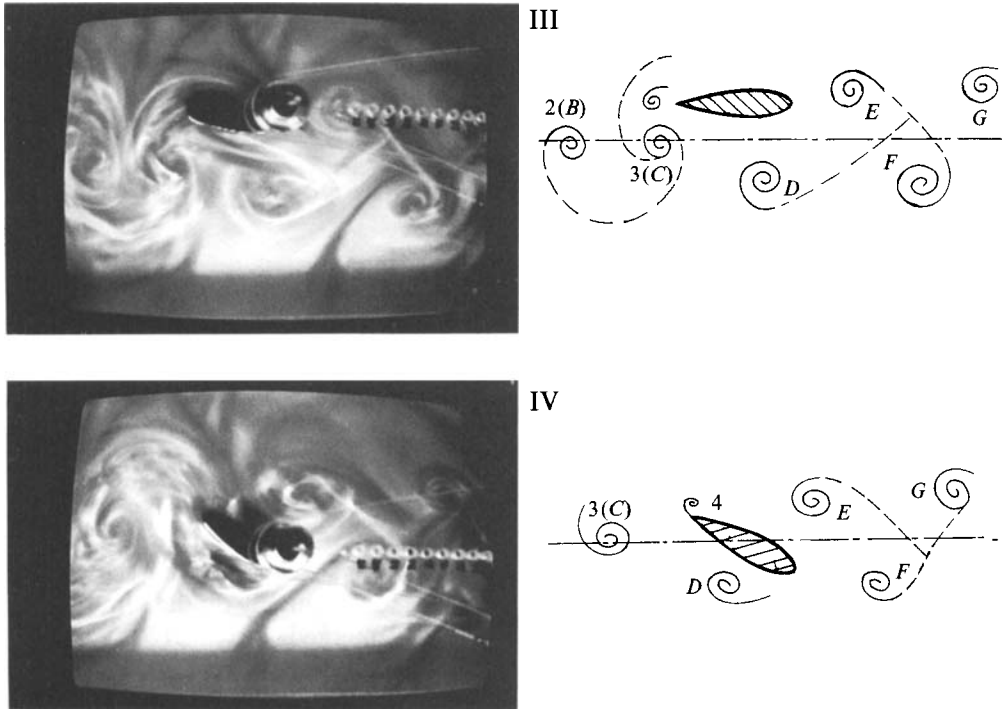


FIGURE 10. Wake interaction mode 3, views III and IV. View III shows the foil at the top of its heave stroke. Foil vortex 3 has grown in size and has merged with the cylinder vortex  $C$ . The combined vortex  $3(C)$  is seen to lie roughly on the same straight line (parallel to the average flow) as the previously merged vortex  $2(B)$ , which has opposite sign and is still visible downstream. View IV shows the foil at the centreline and moving down. The merged vortex  $3(C)$  is well into the wake. From the trailing edge, foil vortex 4 is just forming. Cylinder vortex  $D$  is being swept back below the foil, to eventually merge with vortex 4. Cylinder vortex  $E$  is as yet unaffected by the foil; during the next half-cycle it will be swept back to merge with the next foil vortex, and so on.

shed by the foil; they lie nearly on a straight line in the wake (this is clear in views I and III), and form a reverse Kármán street.

It should be noted that for the case shown the interaction of cylinder vortices with foil vorticity results in the ultimate formation of a reverse Kármán street of vortices with opposite rotational sign relative to the original participating cylinder vortices. Visualization was less clear for this mode than for the other two modes.

### 3.1.3. Mode 3: Constructive interaction

The third mode is characterized by vortex merging as shown in figures 9 and 10. This mode forms a street of single vortices of alternating strength, like mode 2, except that mode 3 results in much strengthened vortices. The vortices are also repositioned and may form a reverse or regular Kármán street.

View I (figure 9) illustrates the situation with the foil at the bottom of the heave stroke. Clearly visible in the wake is the foil vortex 2, which has already merged with the cylinder vortex  $(B)$ . Cylinder vortex  $C$  is located above the foil. View II shows that the merged vortex  $2(B)$  has moved downstream into the wake. Vortex 3 forms at the trailing edge of the foil, which is now at the centreline and moving up. Cylinder vortex  $C$  is swept back over the foil, and will eventually merge with vortex 3. Cylinder vortex  $D$  is as yet too far to be affected by the suction of the foil.

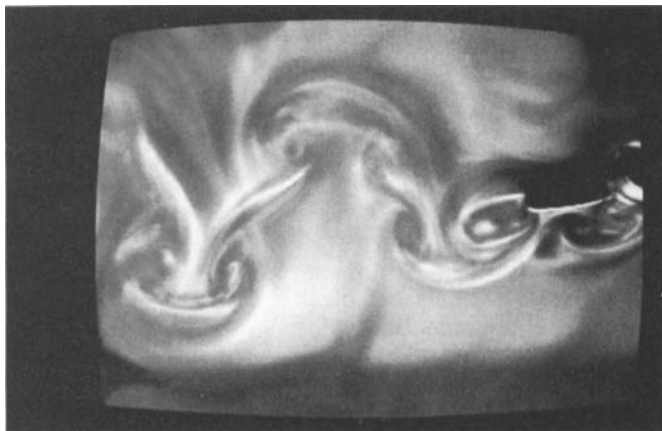


FIGURE 11. Larger view of wake for mode 1, downstream of the foil. Conditions as in figure 5.

The sequence is continued in views III and IV of figure 10. View III shows the foil at the top of its heave stroke. Foil vortex 3 has grown in size and has merged with the cylinder vortex  $C$ . The combined vortex 3( $C$ ) is seen to lie roughly on the same straight line (parallel to the average flow) as the previously merged vortex 2( $B$ ), which has opposite sign and is still visible downstream. View IV shows the foil at the centreline and moving down. The merged vortex 3( $C$ ) is well into the wake. From the trailing edge, foil vortex 4 is just forming. Cylinder vortex  $D$  is swept back below the foil, to eventually merge with vortex 4. Cylinder vortex  $E$  is as yet unaffected by the foil; during the next half-cycle it will be swept back to merge with the next foil vortex, and so on.

### 3.2. Discussion of flow-visualization experiments

The flow-visualization experiments show that the oscillating foil can reposition the vortices, and reduce, or enhance their strength. Repositioning occurs primarily through the action of the foil suction, and can turn, for example, a regular Kármán vortex street (with a wake-like average velocity profile) into a reverse Kármán street (with a jet-like average velocity profile). The process of repositioning can be best seen in modes 2 and 3.

In mode 1 (figure 11) the interaction of the vortex shed by the trailing end of the foil with the vortices of the vortex street seems to follow the general lines of the 'vortex dissolution' process (Aref & Siggia 1981; Aref 1983), as two vortices of opposite sign join up and move outwards from the wake centreline. Also, a similarity can be noted between mode 1 reported herein and the ' $2P$ ' pattern found for certain parametric combinations behind a circular cylinder forced to oscillate harmonically at large amplitude (Williamson & Roshko 1988; Coutanceau & Defaye 1991), although the formation process is totally different in these two cases.

Mode 3 seems to follow the mechanism of 'vortex-pairing' (Aref 1983), as two vortices wrap around each other and form a single structure. Mode 2 involves repositioning of the cylinder vortices by the foil and interaction of a cylinder vortex with vorticity of the opposite sign shed behind the trailing edge of the foil. The detaching shear layer wraps around the oncoming cylinder vortex, as it is repositioned by the foil, ultimately resulting in the formation of one principal vortex per half cycle.

All modes are characterized by the fact that, simultaneously with vortex interaction, significant repositioning of the cylinder vortices takes place, because of the suction of

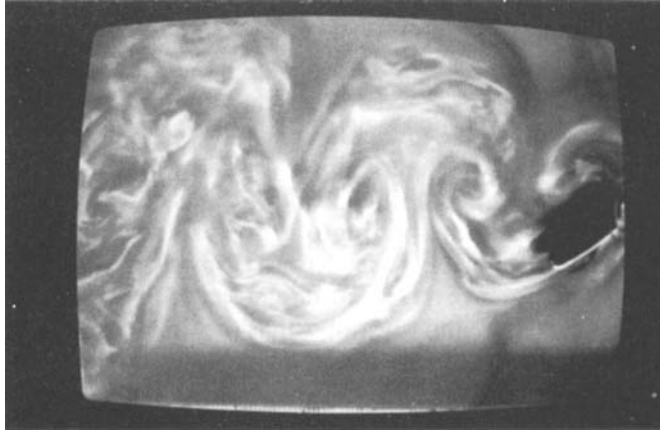


FIGURE 12. Larger view of wake for mode 3, downstream of the foil. Conditions as in figure 9.

the foil. For example, figure 12 shows that in a mode 3 type of interaction, a reverse Kármán street with small lateral spacing is formed downstream of the oscillating foil.

The principal parameter governing the pattern in the wake was found to be the separation distance  $s$  (the separation ratio  $s/d$ ), as shown in figure 4. The separation distance controls the horizontal position of cylinder vortices, relative to the foil pivot point, corresponding to a specific phase in the harmonic motion of the foil. By considering as reference phase the position of the foil with zero heave motion and as it is moving up (which corresponds to a maximum counterclockwise pitch angle in figures 5–10), we find that:

1. In mode 1 the foil attachment point lies midway horizontally between a clockwise and a counterclockwise cylinder vortex.
2. In mode 2 the foil attachment point lies underneath a counterclockwise cylinder vortex. This position is  $+90^\circ$  out of phase with respect to mode 1.
3. In mode 3 the foil attachment point lies above a clockwise cylinder vortex. This position is  $-90^\circ$  out of phase with respect to mode 1.

Of the three modes, vortex pairing was the most sensitive and difficult to reproduce; once formed, however, it produced the clearest images. The destructive and the constructive interaction were both found to be robust and repeatable modes, but they were obtained only for specific values of the separation distance. For parametric values which did not produce one of the three modal patterns just described, the flow was not characterized by any stable repeatable pattern.

In the theoretical study of Dowling (1985), a stationary foil interacts with oncoming vortices near a wall. A single mode of controlled flow is found, where the passage of a vortex near the foil causes the foil to shed vorticity, which reduces the strength of the oncoming vortices. The present study shows that using an oscillating foil offers new possibilities, such as weakening of the circulation (or even reversing), reinforcement of the circulation, and repositioning of the vortices. In Dowling (1985) it is found that the foil chord must have length comparable to the dimension of the oncoming vortex in order to be effective. In the present study it was also found that the foil must have sufficiently large chord to be effective. Two foils were tested, the first with chord length equal to one cylinder diameter, and the second with chord twice as long. The shorter airfoil was found to be very ineffective in controlling the vortices, and all subsequent experiments were conducted with the longer foil. This also led to the use of a similar

foil in the force measurement experiments described in the next section. The lateral spacing of the vortices formed behind the cylinder, before they are altered by the foil, was found to be equal roughly to 2.2 cylinder diameters; hence on the basis of the present results, the foil chord must have a length comparable to the lateral distance between cylinder vortices in order to be effective.

Figures 11 and 12 show a larger part of the wake for modes 1 and 3, respectively, and they serve to demonstrate the stability of the patterns described herein downstream from the foil. Figure 11 shows the pairing of vortices and resulting widening of the wake. Figure 12 shows the vortex street formed downstream of the foil, with the vortices repositioned to form a reverse Kármán street with small lateral spacing. The vortices move from right to left, and one notes that the first (counter-clockwise) vortex, just ahead of the foil, has not been repositioned yet and for this reason is out of line with respect to other vortices of the same sign which have moved downstream from the foil.

#### 4. Force measurement experiments

The experiments were conducted at the MIT Ocean Engineering Testing Tank Facility. The tank has dimensions  $30\text{ m} \times 2.6\text{ m} \times 1.3\text{ m}$ , and is equipped with a computer-controlled carriage rolling on an overhead rail, capable of speeds up to  $3\text{ m s}^{-1}$ .

The apparatus for these force measurement tests is an extension to apparatus used previously for forced-oscillation tests conducted at this facility (Triantafyllou *et al.* 1991, 1993; Gopalkrishnan 1993), but with considerable increase in complexity. Figure 13 illustrates this apparatus, which consisted of two inverted-U yokes each pivoted at its upper end to the carriage. The forward yoke carried the cylinder (D-section) model, while the aft yoke carried the rotating foil model connected via a chain and pulley arrangement to a digitally controlled SEIBERCO motor that provided the pitching oscillation. The aft yoke was similar to the apparatus used by Triantafyllou *et al.* (1991, 1993). Each yoke could be rotated at the pivots and held in position at any angle; thus adjustments to the separation length ratio  $s/d$  were achieved by rotating both yokes through equal and opposite angles either inwards (towards each other) or outwards (away from each other).

Vertical oscillations of the entire assembly were obtained with the use of a second, larger SEIBERCO H3430 Sensorimotor, and a LINTECH leadscrew table of total stroke length 17.8 cm. The base of the device was mounted vertically on the test tank carriage. The motor was digitally controlled.

The cylinder was made of wood with an external layer of glass/graphite fibre for smoothness and strength, 5.08 cm in diameter, 60 cm in span, suspended from the yoke structure by means of stainless steel pins embedded in end plugs. Circular aluminium end plates were fitted, with diameter equal to five times the cylinder diameter, mounted to the lower ends of the yoke arms. One of the arms contained the force transducer. The foil tested has a NACA 0012 shape with zero camber, 10 cm chord and 60 cm span. The foil was made of wood, with an external layer of glass/graphite fibre to ensure uniform smoothness. Circular aluminium end plates of the same size as those for the cylinder were fitted to avoid three-dimensional end effects.

Seven quantities were measured: lift and drag forces on the cylinder, lift and drag forces and torque on the foil, the heaving motion (identical for both models), and the foil pitching motion. The spacing (separation length) between the cylinder and foil models was adjustable. The lift and drag forces on the cylinder and foil models were



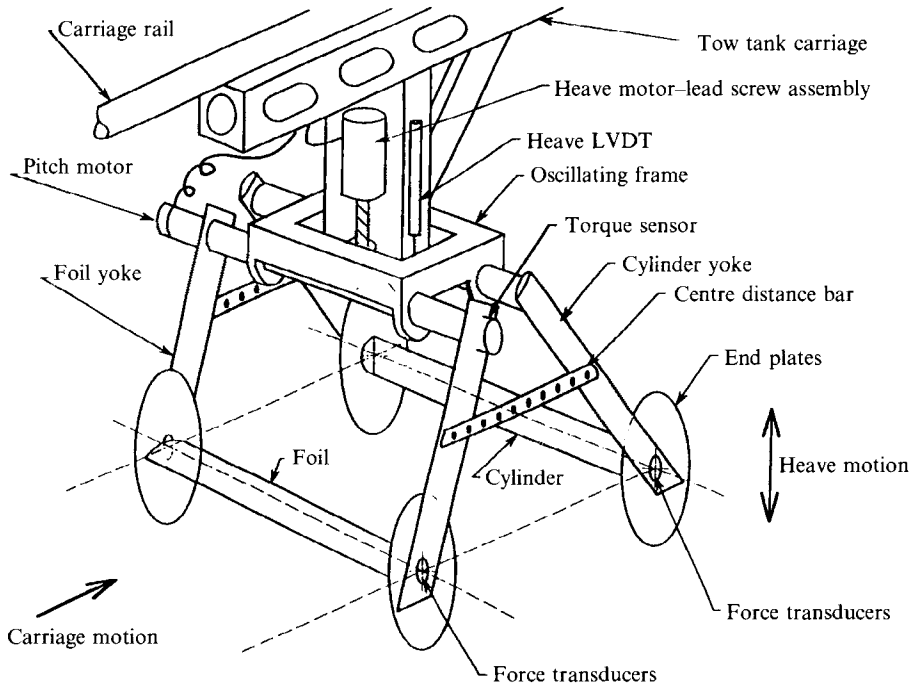


FIGURE 13. Experimental apparatus for force measurement. Two inverted-U yokes carry the cylinder and the foil. One motor drives the heaving motion for both the cylinder and the foil (and attached apparatus) through a lead-screw assembly, and a second motor drives the foil pitching motion through a chain and pulleys.

measured with KISTLER 9117 transducers, while a KISTLER 9065 was used to measure the pitching torque on the foil. A Linear Variable Differential Transformer (LVDT) Model HR 3000, with a linear range of  $\pm 7.62$  cm, was used to measure vertical motion, and a resistance potentiometer was employed to measure the angle of rotation. The seven data signals were transmitted to the control room, filtered, and then sampled by a PC equipped with an A/D converter. A second PC equipped with a D/A converter was used to provide the tracking signals for both the heave and pitch SEIBERCOs as well as the carriage motion.

Both KISTLER transducers and the SCHAEVITZ LVDT were operated with their respective dedicated signal conditioning devices, the charge amplifiers (KISTLER Model 5004) in the case of the force transducers, and a detector/amplifier model ATA 101 in the case of the LVDT. These amplifiers were located on the test tank carriage, so as to be as close as possible to the sensors. The high-level analogue voltages output from the amplifiers were sent back to the laboratory control room, through the test tank data cable connecting the control room to the carriage. From the data cable termination in the control room, the signals were passed through a set of precision matched lowpass analogue filters so as to prevent aliasing. The filters used were built from FREQUENCY DEVICES 4-pole butterworth lowpass modules with a cutoff frequency of 100 Hz, and specifically rigid tolerances on phase- and amplitude-matching.

#### 4.1. Experimental results

The same experimental grid as in table 1 was used for the force measurement experiments. Tests were performed at each amplitude and pitch combination of table 1 and for 14 separation lengths. The separation lengths were chosen to cover at least

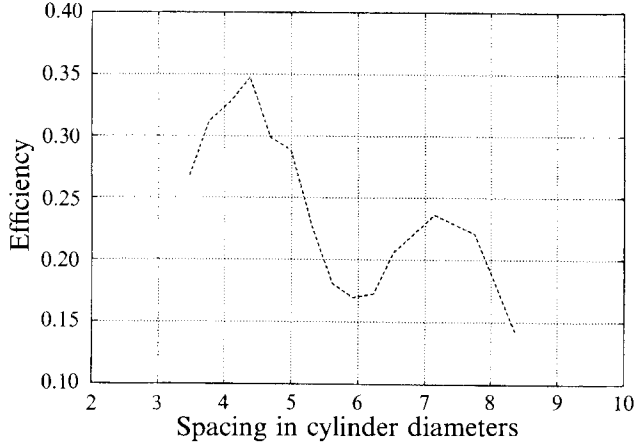


FIGURE 14. Apparent foil efficiency as function of spacing between cylinder and foil.  $A_C/d = 0.833$  and  $\theta = 45^\circ$ .

an entire wavelength in the wake (distance from one cylinder vortex to the next of the same sign), estimated to be between 3.5 diameters (cylinder oscillating with large amplitude), and 5.0 cylinder diameters (non-oscillating cylinder).

From the test data, we extracted values of the cylinder mean drag  $D_{m_C}$ , and the foil thrust (or drag)  $T_{h_F}$ . In addition to the in-line force, we evaluated the average power input to the foil,  $P_F$ , given by:

$$P_F = \left\langle L_F, \frac{dy_F}{dt} \right\rangle + \left\langle Q_F, \frac{d\theta}{dt} \right\rangle, \quad (5)$$

where  $L_F(t)$  is the lift force acting on the foil,  $Q_F(t)$  is the torque on the foil, and  $y_F(t)$  and  $\theta(t)$  are the measured heaving and pitching displacements, respectively. The notation  $\langle x, y \rangle$  denotes the temporal average of the product of the signals  $x(t)$  and  $y(t)$ .

From the measured foil thrust force and input power, we calculated the apparent efficiency  $\eta_F$  of the foil, defined as:

$$\eta_F = \frac{T_{h_F} U}{P_F}, \quad (6)$$

where  $T_{h_F}$  is the average thrust force acting on the foil. We use the term apparent efficiency, because the actual flow velocity at the foil is not measured, and instead the free-stream velocity  $U$  has been used as a reference velocity.

The following conclusions were drawn after plotting the processed data:

1. The cylinder drag force  $D_{m_C}$  did not vary appreciably from the tare value connected with the cylinder alone, nor did it vary much as a function of separation length.

2. The foil thrust force  $T_{h_F}$  was in every case considerably higher than the tare value with the foil alone. The thrust force showed considerable dependence on the spacing.

3. The apparent efficiency of the foil was a strong function of the spacing. This is one of the principal findings of this part of the study.

A typical plot of the experimental results for the efficiency is shown in figure 14 for the case of heave amplitude ratio  $A_C/d = A_F/d = 0.833$  and pitch angle amplitude  $\theta = 45^\circ$ . The foil efficiency is plotted as a function of the separation distance between foil and cylinder, with all other parameters being kept constant. One first notes an average

downward trend in the efficiency as the separation length increases. This is caused by the increase in the average inflow velocity with increasing distance behind the cylinder, owing to the flattening of the average velocity defect. What is remarkable, however, is the presence of distinct peaks in efficiency (one peak at about  $4.3d$ , and another at about  $7.3d$ ), as well as troughs (one trough at about  $6d$  and two additional troughs near the ends of the plotted line in figure 14). These peaks and troughs are caused by the phasing between the arrival of the cylinder vortices and the transverse position of the foil. The distance between peaks in efficiency is roughly equal to the longitudinal distance between vortices of the same sign, estimated at about 3.3 diameters (the value is not precise since the longitudinal vortex spacing varies slowly behind the cylinder).

#### 4.2. Discussion of the force measurement experiments

The results of figure 14 show that the apparent foil efficiency depends strongly on the separation length between cylinder and foil. More specifically, figure 14 shows that the variation of the efficiency of the foil with the separation length presents very clear peaks and hollows. The presence of peaks and hollows suggests that interactions between the oscillating foil and the vortices of the vortex street take place, as also observed in the visualization experiments at lower Reynolds numbers. If no such interactions took place, then the efficiency of the foil would monotonically decrease with the separation distance from the cylinder, as a result of the reduction of the average velocity defect downstream of the cylinder. Instead, figure 14 shows that there is a marked peaking behaviour superimposed on this average reduction. The second effect can only be attributed to the interactions of the foil with the vortices from the upstream cylinder Kármán vortex street.

Since we did not perform flow visualization together with our force measurement apparatus, we cannot definitively correlate the variation in the efficiency of figure 14 with the visualization results discussed earlier. We note, however, that the peak in the efficiency occurred at a spacing of about 4.3 diameters, corresponding roughly with the appearance of mode 2 in the visualization tests (figure 4); while the trough in the efficiency occurred at a spacing of about 6 diameters, corresponding roughly with the occurrence of mode 3 in the  $K$ -tank visualization tests (figure 4). Also, as noted in the previous section, modes 2 and 3 differ by  $180^\circ$ , which corresponds to half a wavelength of the street, in agreement with figure 14 (one wavelength is estimated at 3.3 diameters).

The possibility for energy extraction from the flow was first pointed out by Katzmayer (1922), who considered a stationary foil within an oscillatory flow. Then Schmidt (1965) implemented this by putting a stationary foil behind a flapping foil to increase the overall efficiency. Rosen (1959) visualized the flow around and behind a small swimming fish (*brachydanio albolineatus*, 4.13 cm in length) in a small tank with cross-section  $2.54\text{ cm} \times 3.8\text{ cm}$ , using first a bottom layer of milk with 1.6 mm height, and then dye around the fish. He showed that vortices form around the body of the fish, which are convected downstream with increasing strength and are altered substantially when they interact with the oscillating caudal fin. Similar visualizations are shown in Doi (1989). We suggest, on the basis of the results of the present study, that should these vortices along the fish body be formed, as in the visualizations of Rosen (1959), fish employ a vorticity control scheme similar to mode 2 reported herein, to recover some of the energy lost in forming these vortices. Indeed, multiple sequential photographs of fish swimming show the vortices formed around the body to interact strongly with the flapping tail, resulting in the formation behind the fish of a single dominant vortex street with much weakened vortices, repositioned significantly from their original position to lie in a nearly straight line (Rosen 1959).

## 5. Conclusions

Visualization and force-measurement experiments were conducted to investigate the feasibility of free shear flow control and energy extraction from the large eddies in a free shear flow.

Visualization experiments on a D-section cylinder, oscillating transversely as it is forced to move forward at constant speed, and a heaving and pitching foil, placed behind the cylinder, demonstrated the feasibility of changing the flow through vorticity control. The oncoming vortices of the Kármán street were repositioned and their strength was changed by the foil, resulting in new stable patterns downstream from the foil. Three distinct modes were identified. Mode 1 results in the formation of a street of pairs of counter-rotating vortices, each pair consisting of a vortex from the Kármán street and one generated by the foil. Mode 2 results in the formation of a single vortex street downstream from the foil, each vortex in the street being the result of repositioning by the foil and interaction between a vortex from the Kármán street with vorticity of the opposite rotational sign shed by the trailing edge of the foil. The vortices downstream from the foil may have smaller or even opposite circulation, compared to the circulation of the cylinder vortices before they reach the foil. Mode 3 results in the formation of a single vortex street downstream from the foil, each vortex in the street being the result of merging of a vortex from the Kármán street with a vortex of the same sign generated by the foil, hence having higher strength than the original cylinder vortices. The lateral spacing for the vortex streets of modes 2 and 3 is changed substantially downstream from the foil, and all vortices were roughly lying on a straight line. The principal process in the formation of modes 1 and 3 resembles the two-vortex interaction described in Aref (1983).

Force-measuring experiments on a similar apparatus at larger scale and Reynolds number 20000 demonstrated that, by keeping the excitation conditions the same, but varying the relative spacing between the cylinder and the foil so as to change the arrival time of the cylinder vortices at the foil leading edge to coincide with different phases in the heaving and pitching motion of the foil, the average efficiency of the foil can be altered significantly, with substantial peaks and troughs present. We associate peaks in the efficiency, and hence energy extraction by the foil from the cylinder eddies, with the appearance of mode 2 (destructive interaction); and efficiency troughs with mode 3 (constructive interaction).

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